

# On Language Model Integration for RNN Transducer based Speech Recognition

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#### 1. Introduction

- 2. RNN-Transducer and Internal Language Model
- 3. Experiments
- 4. Conclusion



### End-to-End (E2E) Speech Recognition

• great simplicity and state-of-the-art performance

- popular E2E approaches
  - connectionist temporal classification (CTC) [Graves & Fernández<sup>+</sup> 06]
  - recurrent neural network transducer (**RNN-T**) [Graves 12]
  - attention-based encoder-decoder models [Bahdanau & Chorowski<sup>+</sup> 16, Chan & Jaitly<sup>+</sup> 16]
- models only trained on paired audio-transcriptions

## External Language Model (LM)

- much larger amount of text data
- possibly better-matched domain
- $\rightarrow$  further boost the performance of E2E speech recognition

### **Proper LM Integration ?**



Previously,

- shallow fusion (SF) [Gulcehre & Firat<sup>+</sup> 15a]: simple log-linear model combination
  - widely-used LM integration approach for E2E models
- other sophisticated approaches
  - e.g. deep fusion [Gülçehre & Firat<sup>+</sup> 15b], cold fusion [Sriram & Jun<sup>+</sup> 18]
  - higher complexity but not better than SF

# Recently, Internal Language Model (ILM)

- $\bullet$  RNN-T and attention models
  - context dependency directly included in the posterior distribution
  - implicitly learned sequence prior restricted to the audio transcription only
- strong mismatch with the external LM
- $\rightarrow$  limit the performance of LM integration such as simple SF

# **3 Major Categories to handle ILM**

• **ILM suppression**: suppress ILM in E2E model training

- limiting context/model size [Zeineldeen & Glushko<sup>+</sup> 21]
- introducing an external LM at early stage [Michel & Schlüter<sup>+</sup> 20]

 ILM correction: estimate and correct ILM from the posterior in decoding

 various estimation methods [McDermott & Sak<sup>+</sup> 19, Variani & Rybach<sup>+</sup> 20, Meng & Parthasarathy<sup>+</sup> 21, Zeyer & Merboldt<sup>+</sup> 21, Zeineldeen & Glushko<sup>+</sup> 21]
 fits inte a Payesian interpretation

- fits into a Bayesian interpretation
- **ILM adaptation**: adapt ILM on the same text data used by the external LM
  - train E2E models using text to speech

[Deng & Zhao<sup>+</sup> 21, Kurata & Saon<sup>+</sup> 21, Rossenbach & Zeineldeen<sup>+</sup> 21]

- directly update partial model on text data [Pylkkönen & Ukkonen<sup>+</sup> 21, Meng & Gaur<sup>+</sup> 21]



- ILM suppression
  - complexity: model/training modification
  - performs similarly well as ILM correction [Zeineldeen & Glushko<sup>+</sup> 21]
- ILM adaptation
  - even higher complexity
  - usually aim at restricted application: no external LM
  - with external LM: ILM correction still needed [Deng & Zhao<sup>+</sup> 21]

# • ILM correction

- the most simple and effective LM integration approach
- also a better mathematical justification
- $\rightarrow$  major focus of this work: RNN-T



**RNN-T** Recap

• sequence posterior

$$egin{aligned} P_{\mathsf{RNNT}}ig(a_1^S|Xig) &= \sum_{y_1^{U=T+S}:\mathcal{B}^{-1}(a_1^S)} P_{\mathsf{RNNT}}ig(y_1^U|h_1^Tig) \ &= \sum_{y_1^{U}:\mathcal{B}^{-1}(a_1^S)} \prod_{u=1}^{U=T+S} P_{\mathsf{RNNT}}ig(y_u|\mathcal{B}(y_1^{u-1}),h_1^Tig) \end{aligned}$$

- $a_1^S$ : output (sub)word sequence with  $a \in V$
- X: input acoustic feature sequence
- $-h_1^T = f^{enc}(X)$ : encoder output

-  $y_1^U$ : blank  $\epsilon$ -augmented alignment sequence - unique mapping  $\mathcal{B}(y_1^U) = a_1^S$ : remove all  $\epsilon$ 

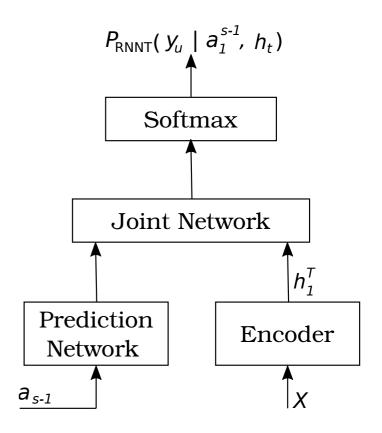


### **RNN-T** Recap cont.

- neural network (NN): parameters  $\theta_{RNNT}$ 
  - encoder: *f*<sup>enc</sup> joint network: *J*
  - prediction network: f<sup>pred</sup>
- lattice representation of RNN-T topology -  $y_1^{u-1}$ : a path reaching a node (t, s - 1)

$$P_{\text{RNNT}}(y_u | \mathcal{B}(y_1^{u-1}), h_1^T) = P_{\text{RNNT}}(y_u | a_1^{s-1}, h_t)$$
  
= Softmax  $\left[ J(f^{\text{pred}}(a_1^{s-1}), f_t^{\text{enc}}(X)) \right]$ 

- 
$$y_1^u$$
: reach  $(t + 1, s - 1)$  if  $y_u = \epsilon$ , or  $(t, s)$  otherwise





Maximum A Posteriori (MAP) Decoding

$$X 
ightarrow \widetilde{a}_1^{\widetilde{S}} = rg\max_{a_1^S,S} Pig(a_1^S|Xig)$$

• no external LM: simply plug in  $P_{\text{RNNT}}(a_1^S|X)$ 

• Bayesian framework: joint integration of the RNN-T model and an external LM – Bayes' theorem: modularized components

$$X \to \tilde{a}_1^{\tilde{S}} = \operatorname*{arg\,max}_{a_1^S,S} P(a_1^S) \cdot P(X|a_1^S) = \operatorname*{arg\,max}_{a_1^S,S} P_{\mathsf{LM}}^{\lambda_1}(a_1^S) \cdot \frac{P_{\mathsf{RNNT}}(a_1^S|X)}{P_{\mathsf{RNNT-ILM}}^{\lambda_2}(a_1^S)}$$

-  $P_{\text{RNNT-ILM}}$ : ILM (sequence prior) implicitly learned and contained in  $P_{\text{RNNT}} \rightarrow$  ILM correction

- $\lambda_1$  and  $\lambda_2$ : scales applied in practice
  - shallow fusion (SF): omit  $P_{\mathsf{RNNT-ILM}}$  with  $\lambda_2=0$





**ILM Estimation** 

• exact  $P_{\text{RNNT-ILM}}$ : intractable marginalization

$$P_{\text{RNNT-ILM}}(a_1^S) = \sum_X P_{\text{RNNT}}(a_1^S|X)P(X)$$

# $\rightarrow$ approximation: estimated $\textit{P}_{\text{ILM}}$

- 2 major trends of estimation
  - statistics of the acoustic training transcription
    - $\rightarrow$  density ratio [McDermott & Sak<sup>+</sup> 19]: train a separate  $P_{\text{ILM}}$  on audio transcription
  - more consistent with the  $P_{\text{RNNT}}$  computation
    - $\rightarrow$  partially reuse the RNN-T NN for computing  $\mathit{P}_{\text{ILM}}$



ILM Estimation: reuse RNN-T NN

$$P_{\mathsf{ILM}}(a_1^S) = \prod_{s=1}^S P_{\mathsf{ILM}}(a_s | a_1^{s-1}) = \prod_{s=1}^S P'(a_s | a_1^{s-1}, h')$$
$$P'(a_s | a_1^{s-1}, h') = \frac{P_{\mathsf{RNNT}}(a_s | a_1^{s-1}, h')}{1 - P_{\mathsf{RNNT}}(\epsilon | a_1^{s-1}, h')} = \mathsf{Softmax} \left[ J_{\backslash \epsilon}(f^{\mathsf{pred}}(a_1^{s-1}), h') \right]$$

- h': some global representation
- P': defined over  $V \rightarrow$  same form as  $P_{\text{RNNT}}$ : usually over  $V \cup \{\epsilon\}$
- simple renormalization
  - instead of separate  $\epsilon$  distribution in  $P_{\text{RNNT}}$ : hybrid autoregressive transducer (HAT) [Variani & Rybach<sup>+</sup> 20]
- $J_{\setminus \epsilon}$ : joint network J excluding the  $\epsilon$  logit output





ILM Estimation: reuse RNN-T NN cont.

$$P_{\mathsf{ILM}}(a_1^S) = \prod_{s=1}^S P'(a_s|a_1^{s-1}, h')$$

$$P'(a_s|a_1^{s-1}, h') = \mathsf{Softmax} \left[ \mathcal{J}_{\backslash \epsilon}(f^{\mathsf{pred}}(a_1^{s-1}), h') \right]$$
1.  $\mathbf{h}'_{\mathsf{zero}} : h' = \vec{0}$  [Variani & Rybach<sup>+</sup> 20, Meng & Parthasarathy<sup>+</sup> 21]  
2.  $\mathbf{h}'_{\mathsf{avg}} : h' = \mathsf{mean}(h_1^T)$  [Zeyer & Merboldt<sup>+</sup> 21, Zeineldeen & Glushko<sup>+</sup> 21]  
3.  $\mathbf{h}'_{\mathsf{a}_1^{s-1}} : h' = f_{\theta_{\mathsf{ILM}}}(a_1^{s-1})$  where  $f_{\theta_{\mathsf{ILM}}}$  is an additional NN  

$$- h'_{\mathsf{mini-LSTM}}$$
 [Zeineldeen & Glushko<sup>+</sup> 21]:  $f_{\theta_{\mathsf{ILM}}} = \mathsf{embedding}_{\mathsf{RNNT}} \circ \mathsf{LSTM}_{50} \circ \mathsf{linear}$ 

$$- \mathsf{training} f_{\theta_{\mathsf{ILM}}} \text{ on audio transcription: } \mathcal{L}_{\mathsf{ILM}} = -\log P_{\mathsf{ILM}}(a_1^S)$$

 $\rightarrow$  combines advantages: transcription statistics + reuse partial RNN-T NN

### Note: these h'-based ILM estimation approaches are based on fixed $\theta_{\text{RNNT}}$



# ILM Training (ILMT)

• *h*'-based ILM approaches: use partial RNN-T NN for  $P_{ILM}$  $\rightarrow$  include ILM into RNN-T model training stage: ILMT

- multi-task training of all parameters including  $\theta_{\rm RNNT}$ 

$$egin{split} \mathcal{L}_{\mathsf{RNNT}} &= -\log P_{\mathsf{RNNT}}(a_1^{\mathcal{S}}|X) \ \mathcal{L}_{\mathsf{ILM}} &= -\log P_{\mathsf{ILM}}(a_1^{\mathcal{S}}) \ \mathcal{L}_{\mathsf{ILMT}} &= \mathcal{L}_{\mathsf{RNNT}} + lpha \mathcal{L}_{\mathsf{ILM}} \end{split}$$

–  $\alpha:$  scaling factor

- originally for the  $h'_{
  m zero}$  approach [Variani & Rybach<sup>+</sup> 20, Meng & Kanda<sup>+</sup> 21]
- also applicable for the  $h'_{avg}$  and  $h'_{a_1}$  approaches





Note: quality of  $P_{ILM} \rightarrow$  how well it matches  $P_{RNNT-ILM}$ 

# Exact-ILM

• recall HAT [Variani & Rybach<sup>+</sup> 20]: h'<sub>zero</sub>-based P<sub>ILM</sub>

$$\begin{array}{ll} \text{if} & J_{\backslash \epsilon} \big( f^{\mathsf{pred}}(a_1^{s-1}), f_t^{\mathsf{enc}}(X) \big) = J_{\backslash \epsilon} \big( f^{\mathsf{pred}}(a_1^{s-1}) \big) + J_{\backslash \epsilon} \big( f_t^{\mathsf{enc}}(X) \big) \\ \text{then} & P_{\mathsf{RNNT-ILM}}(a_s | a_1^{s-1}) \propto \, \exp \left[ J_{\backslash \epsilon} \big( f^{\mathsf{pred}}(a_1^{s-1}), h_{\mathsf{zero}}' \big) \right] \end{array}$$

extension

$$\begin{array}{ll} \text{if} & J_{\backslash \epsilon} \big( f^{\mathsf{pred}} \big( a_1^{s-1} \big), f_t^{\mathsf{enc}} (X) \big) = J' \big( a_1^{s-1} \big) + J_{\backslash \epsilon} \big( f_t^{\mathsf{enc}} (X) \big) \\ \text{then} & P_{\mathsf{RNNT-ILM}} \big( a_s | a_1^{s-1} \big) \propto \, \exp \left[ J' \big( a_1^{s-1} \big) \right] \end{array}$$

- J': any function with output size |V| + independent of X

 $\bullet$  exact-ILM training: train J' to fulfill the assumption  $\rightarrow$  exact ILM estimation

–  $\mathcal{L}_{J'}$ : cross-entropy (CE) loss over Eq. (1)

- simplification: Viterbi alignment of each X + only those  $h_t$  where  $a_s$  occurs



(1)

Exact-ILM cont.

•  $h'_{a_1^{s-1}}$ -based  $P_{ILM}$  + exact-ILM training

$$P_{\mathsf{ILM}}(a_1^S) = \prod_{s=1}^{S} P'(a_s | a_1^{s-1}, h'_{a_1^{s-1}})$$
$$P'(a_s | a_1^{s-1}, h'_{a_1^{s-1}}) = \mathsf{Softmax} \Big[ \underbrace{\mathcal{J}_{\backslash \epsilon}(f^{\mathsf{pred}}(a_1^{s-1}), f_{\theta_{\mathsf{ILM}}}(a_1^{s-1}))}_{\mathcal{J}'(a_1^{s-1})} \Big]$$

- train  $f_{\theta_{\text{ILM}}}$  (fixed  $\theta_{\text{RNNT}}$ )

$$\mathcal{L}_{\mathsf{ILM}}^{\mathsf{exact}} = \mathcal{L}_{\mathsf{ILM}} + \alpha \mathcal{L}_{J'}$$

 $\rightarrow$  theoretical justification:  $P_{\mathsf{RNNT-ILM}}(a_s|a_1^{s-1}) \propto \exp\left[J'(a_1^{s-1})\right]$ 

• other possibilities: e.g. joint training  $\mathcal{L}_{RNNT} + \alpha \mathcal{L}_{J'}$  of all parameters – additionally force the model to better fulfill the assumption  $\rightarrow$  exact ILM estimation



**Decoding Interpretation: why improvement with ILM correction ?** 

$$\begin{split} & \mathcal{K} \to \tilde{a}_{1}^{\tilde{S}} = \operatorname*{arg\,max}_{a_{1}^{S},S} \ P_{\mathsf{LM}}^{\lambda_{1}}(a_{1}^{S}) \cdot \frac{P_{\mathsf{RNNT}}(a_{1}^{S}|X)}{P_{\mathsf{ILM}}^{\lambda_{2}}(a_{1}^{S})} \\ & = \operatorname*{arg\,max}_{a_{1}^{S},S} \sum_{y_{1}^{U}:\mathcal{B}^{-1}(a_{1}^{S})} \prod_{u=1}^{U} P_{\mathsf{RNNT}}(y_{u}|\mathcal{B}(y_{1}^{u-1}), h_{1}^{T}) \cdot Q(y_{u}|\mathcal{B}(y_{1}^{u-1})) \\ & \text{ with } Q(y_{u}|\mathcal{B}(y_{1}^{u-1})) = \begin{cases} 1, & y_{u} = \epsilon \\ \frac{P_{\mathsf{LM}}^{\lambda_{1}}(y_{u}|\mathcal{B}(y_{1}^{u-1}))}{P_{\mathsf{ILM}}^{\lambda_{2}}(y_{u}|\mathcal{B}(y_{1}^{u-1}))}, & y_{u} \neq \epsilon \end{cases}$$

R1. prior removal rebalances label distribution of  $P_{\text{RNNT}}$ 

 $\rightarrow$  rely more on external LM for context modeling (desired)

R2. division by  $P_{\text{ILM}}$  boosts the label probability against (usually high) blank probability

 $\rightarrow$  increase importance of external LM ( $\lambda_1$ ) without suffering huge deletion errors

- limitation of SF ( $\lambda_2 = 0$ ) - no need of decoding heuristics: length-reward ... - however tuning effort in practice: large  $\lambda_2 \rightarrow \text{insertion/substitution errors}$
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### **Experiments**

### Setup

### In-Domain: 960h Librispeech [Panayotov & Chen<sup>+</sup> 15]

- 5k acoustic data-driven subword modeling (ADSM) units [Zhou & Zeineldeen<sup>+</sup> 21]
- strictly monotonic RNN-T (U = T) [Tripathi & Lu<sup>+</sup> 19]
  - 50-dimensional gammatone features [Schlüter & Bezrukov<sup>+</sup> 07]
  - NN structure
    - $f^{enc}$ : 6 × 640 bidirectional-LSTM
    - subsample 4: 2 max-pooling in  $f^{enc}$

- $f^{\text{pred}}$ : embedding $_{256} \circ 2 \times 640 \text{ LSTM}$
- J: linear<sub>1024</sub>-tanh  $\circ$  linear  $\rightarrow$  softmax
- 45 epochs on Librispeech  $\rightarrow$  base model for all experiments
- external LM: 32-layer Transformer

# Cross-Domain: TED-LIUM Release 2 (TLv2) [Rousseau & Deléglise<sup>+</sup> 14]

• external LM: 4 imes 2048 long short-term memory (LSTM)



# Experiments

# Setup cont.

- density ratio LM: same structure as  $f^{\text{pred}}$  + Librispeech transcription
- $h'_{a_1^{s-1}}$  ILM approach:  $h'_{\text{mini-LSTM}}$  with  $f_{\theta_{\text{ILM}}} = \text{embedding}_{\text{RNNT}} \circ \text{LSTM}_{50} \circ \text{linear}_{1280}$ -tanh 1. train  $f_{\theta_{\text{ILM}}}$  with  $\mathcal{L}_{\text{ILM}}$ : 0.5-1 epoch on Librispeech transcription only
  - 2. train  $f_{\theta_{\text{ILM}}}$  with  $\mathcal{L}_{\text{ILM}}^{\text{exact}} = \mathcal{L}_{\text{ILM}} + \alpha \mathcal{L}_{J'}$ : 0.5-1 epoch on Librispeech audio & transcription
    - Viterbi alignment using the base RNN-T model
    - $\scriptstyle \bullet \alpha: 1.0$  for in-domain evaluation and 2.0 for cross-domain evaluation
- ILMT:  $\mathcal{L}_{ILMT} = \mathcal{L}_{RNNT} + \alpha \mathcal{L}_{ILM}$  with  $\alpha = 0.2$ 
  - applied for  $h'_{\text{zero}}$ ,  $h'_{\text{avg}}$  and  $h'_{\text{mini-LSTM}}$  ILM approaches
  - initialize with base RNN-T model + fine-tune upto 10 epochs on Librispeech
  - $\mathcal{L}_{ILM}$  only relevant for  $f^{pred}$  and J: freeze  $f^{enc}$
- alignment-synchronous decoding [Saon & Tüske<sup>+</sup> 20]
  - score-based pruning + beam limit 128
  - no heuristic approach: effect of each LM integration method
  - scales optimized on dev sets



### LM Integration Evaluation

Madal	Evaluation	Li	ibrispee	TLv2 wer [%]			
Model Train		dev		test		dev	test
		clean	other	clean	other	ucv	lest
$\mathcal{L}_{RNNT}$	no LM	3.3	9.7	3.6	9.5	19.8	20.3
	SF	2.0	5.1	2.2	5.5	15.5	16.4
	density ratio	1.9	4.8	2.1	5.2	14.1	15.0
	$h'_{ m zero}$	1.8	4.4	2.0	4.8	13.6	14.4
	$h'_{ m avg}$	1.8	4.4	2.0	4.9	13.5	14.6
$+ \mathcal{L}_{ILM}$		1.8	4.3	1.9	4.7	13.4	14.4
$+ \mathcal{L}_{ILM}^{exact}$	$h'_{\rm mini-LSTM}$	1.8	4.2	1.9	4.6	13.2	14.0
$\mathcal{L}_{ILMT}$	h' <sub>zero</sub>	1.8	4.4	2.0	4.8	13.3	14.2
	h' <sub>avg</sub>	1.9	4.5	2.1	4.9	13.5	14.4
	$h'_{\rm mini-LSTM}$	1.8	4.4	2.0	4.8	13.2	14.1

- external LM: significant gain
- ILM correction: further large improvement over SF
- h'-based approaches: better than density ratio
  - $-h'_{\text{mini-LSTM}}$   $(h'_{a_1^{s-1}})$ : best
- proposed  $\mathcal{L}_{ILM}^{exact}$ : further improve  $h'_{mini-LSTM}$ 
  - also better than  $\mathcal{L}_{\mathsf{ILMT}}$
- $\mathcal{L}_{\text{ILMT}}$ : little effect on Librispeech
  - decreasing L<sub>ILM</sub>: no improvement
     on the overall performance
     (HAT [Variani & Rybach<sup>+</sup> 20])



#### **Experiments**

**Verification: 2 decoding-perspective reasons for improvement with ILM correction** R1. rebalance label distribution: rely more on external LM for context modeling R2. boost label probability: increase importance of external LM ( $\lambda_1$ ) without huge deletion errors

- individual effect of R2 without effect of R1: SF + length reward
- individual effect of R1 without effect of R2:  $h'_{\text{zero}}$  + renorm- $\epsilon$ 
  - for each  $y_u \neq \epsilon$ 
    - 1. renormalization:

$$P_{\text{norm}}(y_u) = \frac{P_{\text{RNNT}}(y_u | \mathcal{B}(y_1^{u-1}), h_1^T) / P_{\text{ILM}}^{\lambda_2}(y_u | \mathcal{B}(y_1^{u-1}))}{\sum_{a \in V} P_{\text{RNNT}}(a | \mathcal{B}(y_1^{u-1}), h_1^T) / P_{\text{ILM}}^{\lambda_2}(a | \mathcal{B}(y_1^{u-1}))}$$

2. modify probability for search:

$$(1 - P_{\mathsf{RNNT}}(\epsilon | \mathcal{B}(y_1^{u-1}), h_1^{\mathsf{T}})) \cdot P_{\mathsf{norm}}(y_u) \cdot P_{\mathsf{LM}}^{\lambda_1}(y_u | \mathcal{B}(y_1^{u-1}))$$

– restrict label probability w.r.t.  $\epsilon$  + maintain rebalanced label distribution to some extent



Verification: 2 decoding-perspective reasons for improvement with ILM correction R1. rebalance label distribution: rely more on external LM for context modeling R2. boost label probability: increase importance of external LM ( $\lambda_1$ ) without huge deletion errors

Evaluation	$\lambda_1$	$\lambda_2$	Librispeech dev-other				• SF $+$ length r
Evaluation			WER	Sub	Del	Ins	$\rightarrow$ verify R2
SF	0.61	Ο	5.1	3.8	0.9	0.4	• $h'_{ m zero}$ + renorm
+ length reward	0.65	U	4.8	3.8	0.5	0.5	0
$h'_{\sf zero} + {\sf renorm} - \epsilon$	0.61	0.35	4.9	3.6	0.9	0.4	$\rightarrow$ verify R1
+ length reward	0.65	0.55	4.6	3.7	0.5	0.4	• $h'_{ m zero}$ + renorm-
h' <sub>zero</sub>	0.85	0.4	4.4	3.5	0.5	0.4	• <i>h</i> ′ <sub>zero</sub> : enlarge l
+ length reward	0.95	0.4	4.5	3.6	0.5	0.4	– further impr

- reward: reduced deletion errors 2 without R1
- n- $\epsilon$ : reduced substitution errors, but tion errors

without R2

- $-\epsilon + \text{length reward: complementary}$
- R1 and R2 with larger scales
  - rovement
  - length reward not needed



- RNN-T LM integration: mismatch between external LM and ILM  $\rightarrow$  ILM correction
- detailed formulation: various ILM correction-based methods in a common RNN-T framework
- decoding interpretation: 2 major reasons for performance improvement with ILM correction
   experimentally verified with detailed analysis
- exact-ILM training framework: extension upon HAT
  - theoretical justification for different ILM approaches
- systematic comparison: in-domain Librispeech and cross-domain TLv2
  - $-h'_{\text{mini-LSTM}}(h'_{a_1^{s-1}})$ : best
  - -+ exact-ILM training: further improvement

# Thank you for your attention



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